## Vehicle Accident Analysis and Reconstruction Methods

## Raymond M. Brach and R. Matthew Brach, SAE, 2005 First Printing

August 10, 2012

| page | Eq/Line | Correction |
| :---: | :---: | :---: |
| 33 | (2.32) | $F_{y}(\alpha, s)=\frac{F_{x}(s) F_{y}(\alpha)}{\sqrt{s F_{y}^{2}}(\alpha)+F_{x}(s)} \frac{\sqrt{(1-s)^{2} \cos ^{2} \alpha F_{y}^{2}(\alpha)+\sin ^{2} \alpha C_{s}^{2}}}{}$ |
|  | (2.32) | $F_{y}(\alpha, s)=\frac{F^{2}}{\sqrt{s^{2} F_{y}^{2}(\alpha)+F_{x}^{2}(s) \tan ^{2} \alpha}} \quad C_{s} \cos \alpha$ |
| 41 | line 3 | $\tau=\frac{-11.11}{-7.86}=1.4 \mathrm{~s}$ |
| 41 | line 4 | . . . skids to a stop in 1.4 s . . . |
| 45 | line 24 | $f_{r}=\frac{F_{t r}}{F_{z r}}=\frac{T / R_{w}}{F_{z r}}=\frac{1935 / 0.34}{13947}=0.408$ |
| 48 | line 9 | calculation for $\mu_{\mathrm{s}}$ has units $\mathrm{ft} / \mathrm{s}$ |
| 49 | line 3 | $\sigma_{d}=v_{0} \sigma_{\text {PDR }}=44 \times 0.833=3.65 \mathrm{ft}$ |
|  | line 5 | $\sigma_{t}=\sigma_{\text {PDR }}=0.83 \mathrm{~s}$ |
|  | line 8 | ...and a standard deviation of 0.83 s . |
| 47 | Ex 3.4 | grade is $5^{\circ}\left(f_{\text {eq }}=0.585\right)$ |
| 60 | line 25 | $F_{y}(s) \approx f_{y} F_{z}$ |
|  | (4.8) | $F_{y}(\alpha, s) \approx f_{y} F_{z}$ |
|  | (4.9) | $F_{x}(\alpha, s) \approx 0$ |
| 69 | (5.2) | $f_{E}=f_{t} \sin \alpha+f_{p} \cos \alpha+\sin \theta$ |
| 77 | Eq 5.8 | $\frac{1}{2} I_{0} \dot{\theta}^{2}=m g\left(\sqrt{\left(\frac{T}{2}\right)^{2}+h^{2}}-h\right)$ |
| 77 | Eq. 5.6 | $V=\sqrt{2 g h \sqrt{\left(\frac{T}{2 h}\right)^{2}+1}-1}$ |
| 85 | line 8 | . . . using Eq. 5.15 |
| 93 | last - 4 | . . . lated using Eq. 5.15. |
| 93 | last | using Eq 5.12. |
| 94 | line 1 | Equation 5.12 is used... |
| 94 | line 5 | (Eq. 5.13) |

## Comment

subscript, s , and superscript, 2 , missing on C
incorrect number in denominator
skid time is 1.4 s , not 1.3 s
$F_{t r}$ should be torque, $T$, divided by the rolling radius $R_{w}$
units should be ft not $\mathrm{ft} / \mathrm{s}$
$\sigma_{d}=v_{0} \sigma_{\mathrm{PDR}}=44 \times 0.0833=3.65 \mathrm{ft}$
$\sigma_{t}=\sigma_{\mathrm{PDR}}=0.083 \mathrm{~s}$
...and a standard deviation of 0.083 s .
grade is not $5 \%$
symbol for frictional drag coefficient is $f$, not $\mu$
no subscript on $\alpha$; frictional drag coefficient is $f$
no subscript on $\alpha$
subscript on last $f$ should be $p$
$\dot{\theta}$ should be squared
the 1 under the second square root should be positive
the equation number should be 5.15 , not 5.16
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cited equation should be Eq. 5.13, not Eq. 5.14
last
$=9.18 \mathrm{~m} / \mathrm{s}$ should $\mathrm{be}=-9.18 \mathrm{~m} / \mathrm{s}$
(6.27) $\quad e_{k}=\sqrt{\frac{e_{1}^{2} k_{2}+e_{2}^{2} k_{1}}{k_{1}+k_{2}}}$
(6.65b) $\quad+\frac{1}{2} P_{t}\left[\left(v_{1 t}-d_{d} \omega_{1}\right)-\left(v_{2 t}+d_{b} \omega_{2}\right)+\left(V_{1 t}-d_{d} \Omega_{1}\right)-\left(V_{2 t}+d_{b} \Omega_{2}\right)\right]$
fig 7.16 units of speed for solid curve are $\mathrm{ft} / \mathrm{s}$
last $\quad$. . .range of $5.22 \mathrm{ft} / \mathrm{s}$ to $6.07 \mathrm{ft} / \mathrm{s}(2.3 \mathrm{~m} / \mathrm{s}$
first $\quad .$. . range of $-4.31 \mathrm{ft} / \mathrm{s}$ to $-4.93 \mathrm{ft} / \mathrm{s}(-1.9 \mathrm{~m} / \mathrm{s}$ to
last . . in Chapter 11. should be . . in Reference 6 of Chapter 7.
Sol'n A $\quad V=43.8 \mathrm{mph}(64.2 \mathrm{ft} / \mathrm{s}, 70.5 \mathrm{kph})$
Sol'n B $\quad ., C=0$ occurs at a speed of $V=6.85 \mathrm{mph}(10.1 \mathrm{ft} / \mathrm{s}$, $11.0 \mathrm{kph})$, when the kinetic energy is $7059.9 \mathrm{ft}-\mathrm{lb}(9.57 \mathrm{~kJ})$.

$$
\begin{aligned}
d_{0} & =\sqrt{\frac{2(7059.5)}{6.58}}=46.31, l b^{1 / 2} \\
d_{1} & =\frac{1}{C}\left(\sqrt{\frac{2 E_{C}}{w}}-d_{0}\right)=\frac{1}{3.5}\left(\sqrt{\frac{2(288,631)}{6.58}}-46.31\right) \\
& =71.39 \mathrm{lb} b^{1 / 2} / \mathrm{ft}\left(4.59 \mathrm{~N}^{1 / 2} / \mathrm{cm}\right)
\end{aligned}
$$

line $21 \ldots$ should not be computed by Eq 8.10.
line 12 Equation 8.14 gives $d_{l} \ldots$
line 6 ... methods, but this is not done here.
last-5 $\quad \ldots$ from $\tau=\tau_{0}$ to $\tau=\tau_{\mathrm{c} 1} \ldots$
Eq 9.9 $\quad \tau_{R}=\frac{v_{p 0} \sin \theta}{g \cos \varphi}+\frac{\sqrt{\nu_{p 0}^{2} \sin ^{2} \theta+2 g h \cos \varphi}}{g \cos \varphi}$
line 4 ... two lines in three dimensional space.
(10.4b) $y_{m}=\frac{c_{6}+c_{7} x_{p}+c_{8} y_{p}}{c_{4} x_{p}+c_{5} y_{p}+1}$

T 4, line 4 Insert: No more than two of the four points can be collinear. Sentence was omitted.

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| 125 | (6.65b) | $+\frac{1}{2} P_{t}\left[\left(v_{1 t}-d_{d} \omega_{1}\right)-\left(v_{2 t}+d_{b} \omega_{2}\right)+\left(V_{1 t}-d_{d} \Omega_{1}\right)-\left(V_{2 t}+d_{b} \Omega_{2}\right)\right]$ |
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| 151 | first | .. .range of $-4.31 \mathrm{ft} / \mathrm{s}$ to $-4.93 \mathrm{ft} / \mathrm{s}(-1.9 \mathrm{~m} / \mathrm{s}$ to |
| 154 | Sol'n A | $V=43.8 \mathrm{mph}(64.2 \mathrm{ft} / \mathrm{s}, 70.5 \mathrm{kph})$ |

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$\dot{\theta}$ should be squared
the 1 under the second square root should be positive
the equation number should be 5.15 , not 5.16
missing square root sign
$V_{2 t}$ in second parenthesized term should be lower case
units should be $\mathrm{ft} / \mathrm{s}$ not mph units should be ft/s not mph units in the equation in Figure 8.1 are mph

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$$
\text { last-5 } \quad \ldots \text { from } \tau=\tau_{0} \text { to } \tau=\tau_{c l} \ldots
$$

$$
\text { Eq } 9.9 \quad \tau_{R}=\frac{v_{0} \sin \theta}{g \cos \varphi}+\frac{\sqrt{v_{o p}^{2} \sin ^{2} \theta+2 g h \cos \varphi}}{g \cos \varphi}
$$

- 4, line 4 Insert: No more than two of the four points can be collinear.
units in the equation in Figure 8.1 are mph
$s_{1}$ begins when $s_{0}$ ends
second equal sign should be a plus sign
Sentence was omitted.

